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RF Energy Harvesting in Wireless Networks with HARQ

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Outline

Motivation

- Wireless Energy Harvesting (WEH)
- System Model

Proposed Energy Harvesting Policies

- Time Switching when CSI is unavailable
- Time Switching policies when CSI is available

Numerical results

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A promising Solution for Limited Power Wireless Networks

- ▶ Ideally, WEH provides an unlimited supply of energy.
E.g., Sensor Networks.
- ▶ Ambient radio frequency (RF) transmissions can be harvested for energy.
 - ▶ Motivates studying Simultaneous Wireless Power and Information Transfer (SWIPT).

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Challenges of Wireless Communications Channels

Wireless channel gain fluctuates over time causing outages

- ▶ Hybrid Automatic Repeat Request (HARQ).

- ▶ Message is encoded by a mother code of rate R .

- ▶ Divided into N codewords, transmitting each consecutively until receiver can decode the message.

- ▶ What is the interplay of HARQ re-transmissions and RF energy harvesting for a receiver without any other power source?

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Contributions

- ▶ Analyze trade-off between accumulating mutual information and harvesting RF energy at the receiver of a point-to-point link using HARQ.
- ▶ Characterize the optimal time switching (TS) policy to maximize the probability of successful message decoding,
 - ▶ where TS policy decides to harvest energy or accumulate information at every slot
 - ▶ when the channel state information (CSI) is /and is not used by the receiver for making TS decision,

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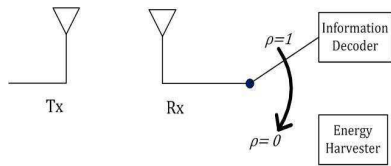
Time Switching when CSI is unavailable

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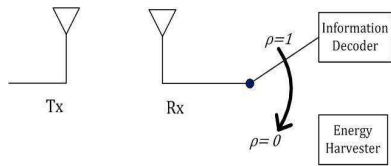
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- ▶ Transmitter has power supply.
- ▶ Receiver harvests energy from the received RF signal.
- ▶ Time is slotted.
- ▶ Rayleigh flat fading wireless channel.
- ▶ Transmitter employs HARQ protocol.



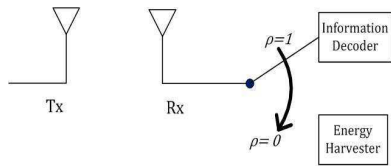
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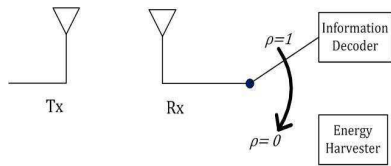
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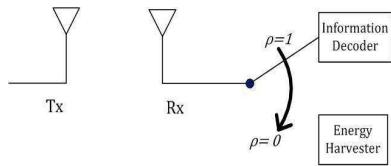
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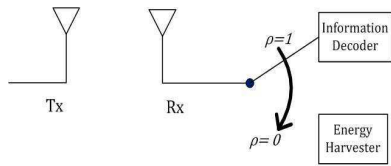
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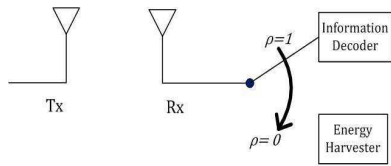
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- ▶ Maximum number of message re-transmissions is N .
- ▶ Fixed transmission power P per slot.
- ▶ ρ_t is time switching decision at time slot t .
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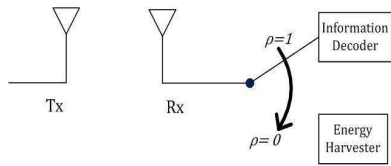
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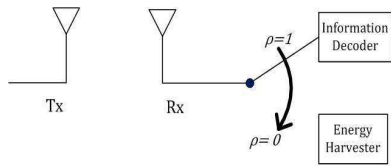
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Dynamic Program (DP) Formulation

- ▶ Consider the action at time slot t to be time switching decision ρ_t ,

$$\mathbf{a}_t = \rho_t = \begin{cases} 0, & \text{for RF energy harvesting} \\ 1, & \text{for information decoding} \end{cases} \quad (1)$$

- ▶ System state $\mathbf{s}_t = (f_t, g_t)$,

$$f_t = \sum_{k=1}^{t-1} \log(1 + \rho_k P h_k), \quad (2)$$

$$g_t = \sum_{k=1}^{t-1} (1 - \rho_k) P h_k, \quad (3)$$

- ▶ Reward $x_t(\mathbf{s}, a)$ of 1 when message is decoded, i.e.,

$$x_t(\mathbf{s}, a) = \begin{cases} 1 & \text{if } (f_t + \log(1 + \rho_t P h_t) \geq R) \\ & \cdot \mathbb{I}(g_t + (1 - \rho_t) P h_t \geq \zeta), \end{cases} \quad (4)$$

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- ▶ A closed form solution of DP with continuously varying states is intractable.
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Greedy Time Switching Algorithm

- ▶ Computationally efficient greedy policy with good performance results.
- ▶ The decision policy, ρ_t^* , minimizes the probability of decoding failure at time slot t ,

$$\rho_t^* = \begin{cases} 0, & \text{if } 2^{fr_t} - 1 \geq gr_t, \\ 1, & \text{Otherwise.} \end{cases} \quad (5)$$

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Sub-optimal TS Policy (*STSP* – *CSI*)

- ▶ **Observation:** Including the instantaneous channel gains significantly increases the computational complexity of the DP.
- ▶ A simple heuristic TS policy inspired by the previous DP formulation.
- ▶ **Remarks:**
 - ▶ Receiver either collects the required mutual information or energy in a time slot, whichever has the higher probability of successful decoding depending on the channel gain.
 - ▶ If both memory and battery thresholds cannot be met in the current slot, storing mutual information always results in a higher probability of successful decoding.

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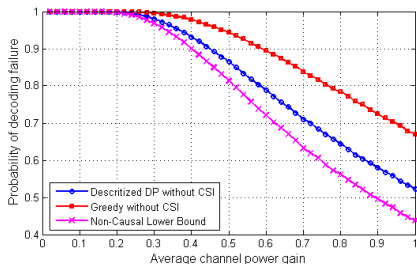
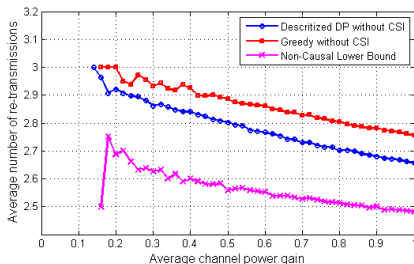
Greedy Time Switching Algorithm

- ▶ When the instantaneous CSI is available for TS decision, we design a greedy TS policy that aims to minimize the decoding failure probability in the subsequent slot
 - ▶ **Remark:** Failure is either due to insufficient mutual information accumulation or insufficient battery level.
- ▶ The optimal decision taken at every slot is given by,

$$\rho_t = \begin{cases} 1, & \text{if } \frac{2^{f_t}}{1+h_t P} \geq 2^{f_t} - h_t P, \\ 0, & \text{Otherwise.} \end{cases} \quad (6)$$

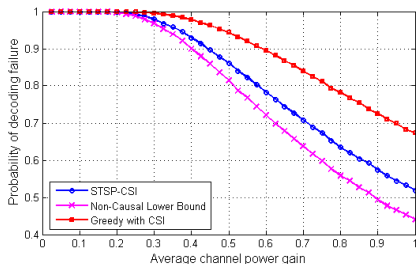
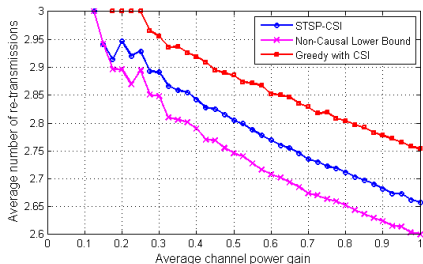
CSI not available for TS decision

- ▶ Max transmissions is 3, $R=1$, $P=1$, the required energy to decode is $0.8 \cdot P$. Average over 10^5 runs.



- ▶ The non-causal policy has all future channel state information for making TS decisions.
- ▶ Channel is discretized into 50 states, resulting in an approximate channel behavior.

CSI available for TS decision



- ▶ Unlike the previous case, the channel state is not discretized, giving smoother and more accurate results.

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- ▶ When CSI at the receiver is **unavailable**.
 - ▶ Formulated a dynamic programming problem.
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Future Directions

- ▶ Future research should address the following:
 - ▶ The assumption of infinite capacity for both energy and information is ideal.
 - ▶ The receiver power consumption should also be taken into account.
 - ▶ The potential extension to the general case with multiple users.